



# Bigraphical models for Container-based Systems

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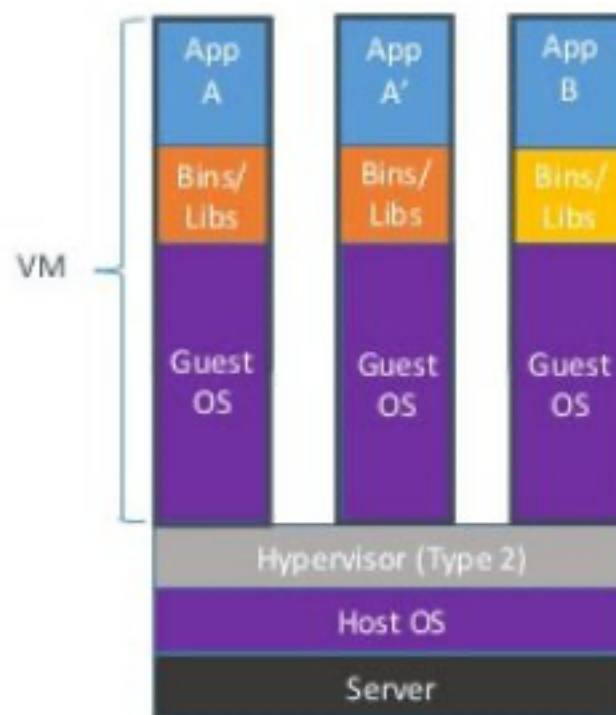
## Microservice-oriented architectures...

- **Microservice:** A highly cohesive, single purpose and decentralized service
- **Microservice-oriented architecture**
  - Applications are built by composing microservices through **interfaces (APIs)**
  - Distributed component-based
  - Flexible, scalable, supporting dynamic deployment and reconfiguration, agile prog., etc.

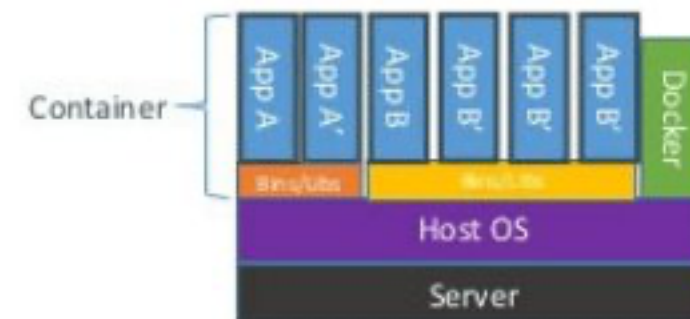


## ... and containers

- **Containers** are widely used for implementing Microservices
  - Ensure execution separation (leveraging kernel namespaces and cgroups in the host OS) separation of tasks, portability
  - **Clear definition of interfaces**
  - Support service and component **composition**
  - Lighter than virtual machines



Containers are isolated, but share OS and, where appropriate, bins/libraries



# Containers can be filled with libraries, code, data...

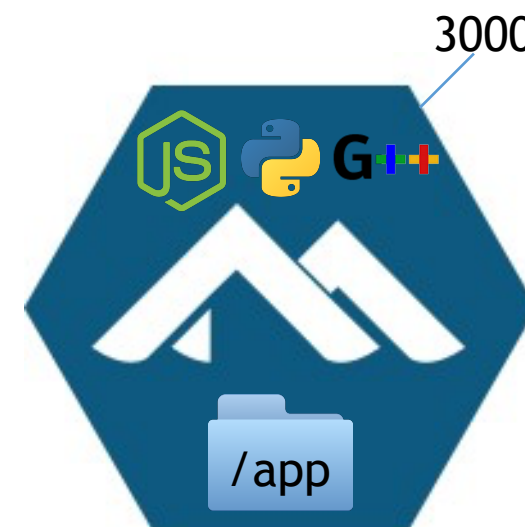
- **Dockerfiles:** recipes to build *images*.

Example:

- Start from an existing image
- Run any command, e.g. to extend the image with any needed package
- Install programmer's specific code
- Define the entry point command (what to execute when the container is launched)
- Declare exposed ports (interfaces)
- These recipes are fed to `docker build`
- Result: a **new image**, which can be run in a container, or used as basis for further builds
- (We will not discuss dockerfiles in this talk)



```
# syntax=docker/dockerfile:1
FROM node:12-alpine
RUN apk add --no-cache python2 g++ make
WORKDIR /app
COPY . .
RUN yarn install --production
CMD ["node", "src/index.js"]
EXPOSE 3000
```

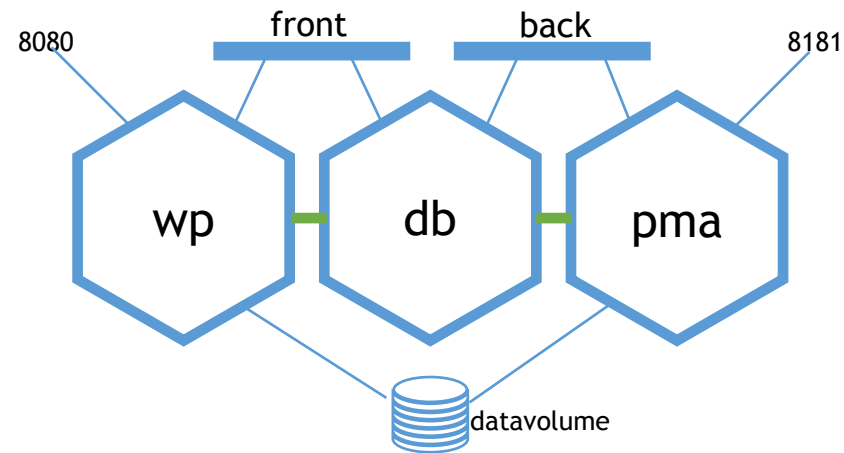


## ...and connected to other containers through their interfaces

- Composition is defined by YAML files declaring
  - (Virtual) Networks
  - Volumes (possibly shared)
  - For each container
    - Name
    - Images
    - Networks which are connected to
    - Port remappings
    - Volumes
    - Links between services
- Configuration file is fed to an *orchestration* tool (docker compose) which downloads the images, creates the containers, the networks, the connections, etc. and launches the system

```
services:  
  wp:  
    image: wordpress  
    links:  
    - db  
    ports:  
    - "8080:80"  
    networks:  
    - front  
    volumes:  
    - datavolume:/var/www/data:ro  
  db:  
    image: mariadb  
    expose:  
    - "3306"  
    networks:  
    - front  
    - back
```

```
pma:  
  image: phomyadmin/phpmyadmin  
  links:  
  - db:mysql  
  ports:  
  - "8181:80"  
  volumes:  
  - datavolume:/data  
  networks:  
  - back  
networks:  
  front:  
    driver: bridge  
  back:  
    driver: bridge  
volumes:  
  datavolume:  
    external: true
```



# Vertical vs Horizontal Composition

- Containers can be composed to form larger systems
- Two different compositions:
  - **Vertical\***: containers can be filled with application specific code, processes... (by developers or at deployment)
  - **Horizontal\***: containers are on a par, and communicate through channels (sockets, API), volumes, networks

\* = my naming, not official

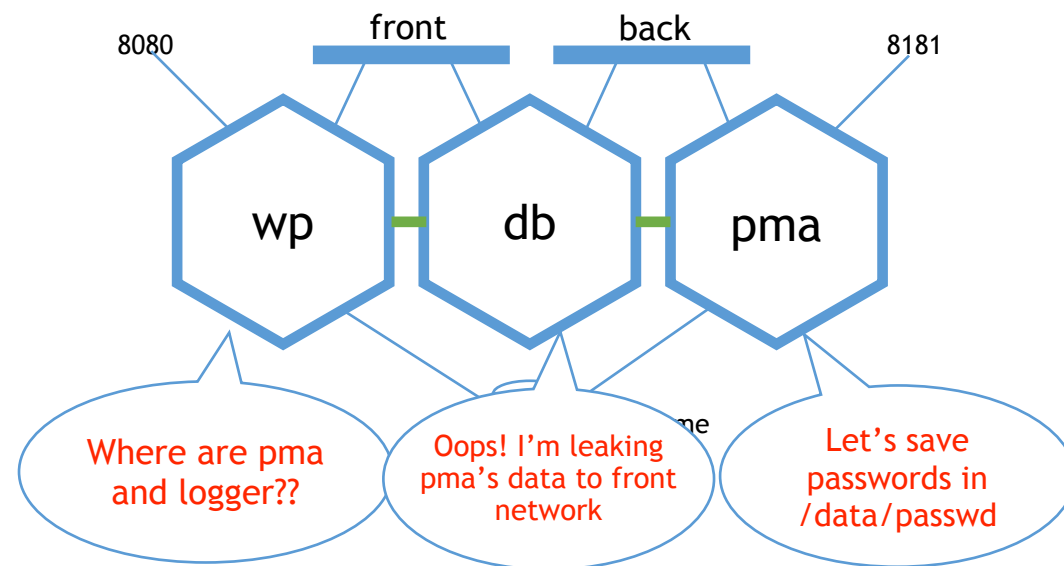


# What if a composition configuration is not *correct*?

- A configuration may contain several errors, which may lead to issues during **composition**, or (worse) at **runtime**.

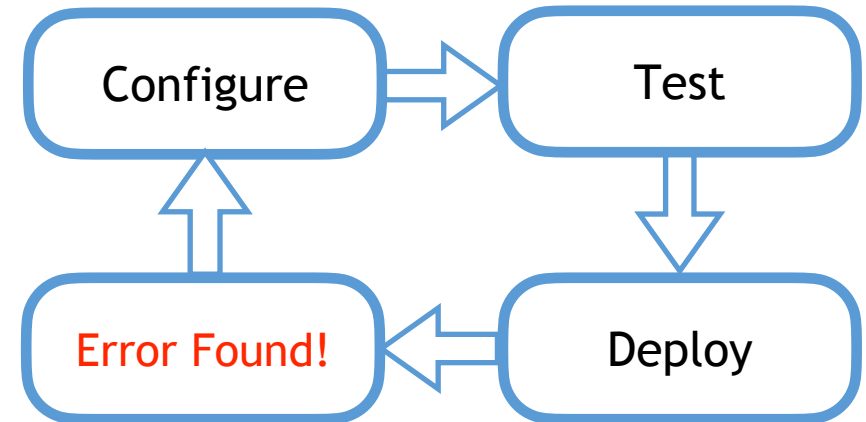
E.g.:

- A container may try to access a **missing services**, or a service which is not connected to by a network
- Ambiguous declaration of services
- **Security policies** violations, e.g. sharing networks or volumes which should not (or only in a controlled way) leading to information leaks
- **Dynamic reconfiguration** can break properties previously valid
  - Container's images can be updated at runtime (e.g. for bug fixing)
  - Adding or removing containers to an existing and running system



## What if a composition configuration is not *correct*?

- Actual composition tools check only very basic aspects
- Common approach: *try-and-error*
  - Expensive
  - Slow
  - Not scalable
  - Not safe enough
- Not acceptable in critical situations
- We need tools for analyzing, verifying (and possibly manipulate) container configurations
  - Before executing the system (static analysis), or at runtime





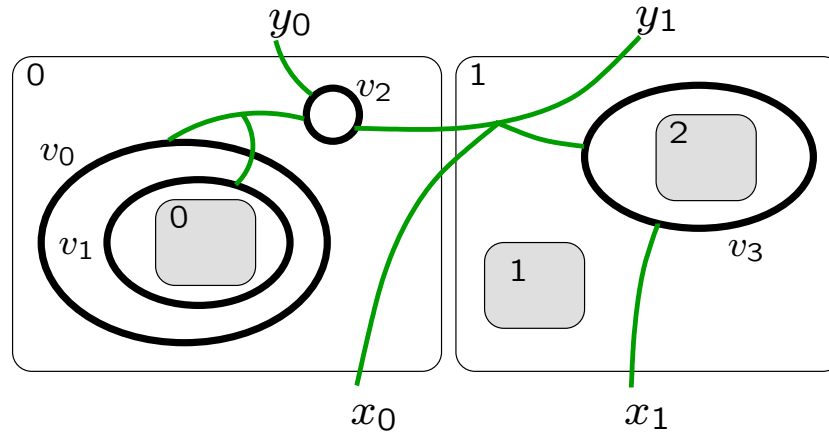
## Serious tools need solid theoretical foundations

- We need a *formal model of containers and services composition*
- This model should support:
  - Logical connections of components
  - Horizontal **Bigraphs (Milner, 2003):** a general model for distributed components
  - Dynamic reconfiguration (meta)model for distributed communicating systems, supporting **composition and nesting.**
  - Different granularities
  - Flexibility
  - Openness (we may need to add more details afterwards)
  - ...

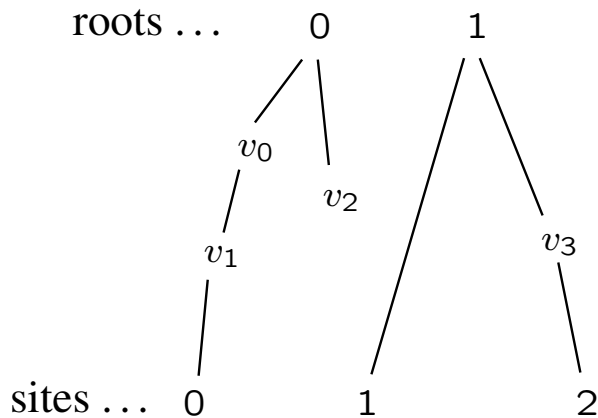
# Quick intro to bigraphs [Milner, 2003]

- A bigraph consists of hyperedges and nodes that can be *nested*. Each hyperedge can connect many ports on different nodes.

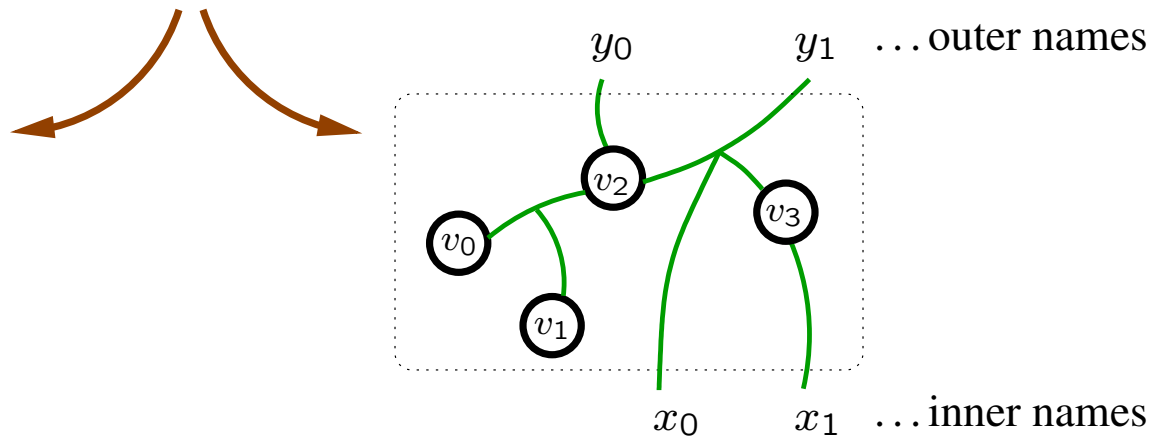
**bigraph**  
 $G: \langle m, X \rangle \rightarrow \langle n, Y \rangle$



**place graph**  
 $G^P: m \rightarrow n$

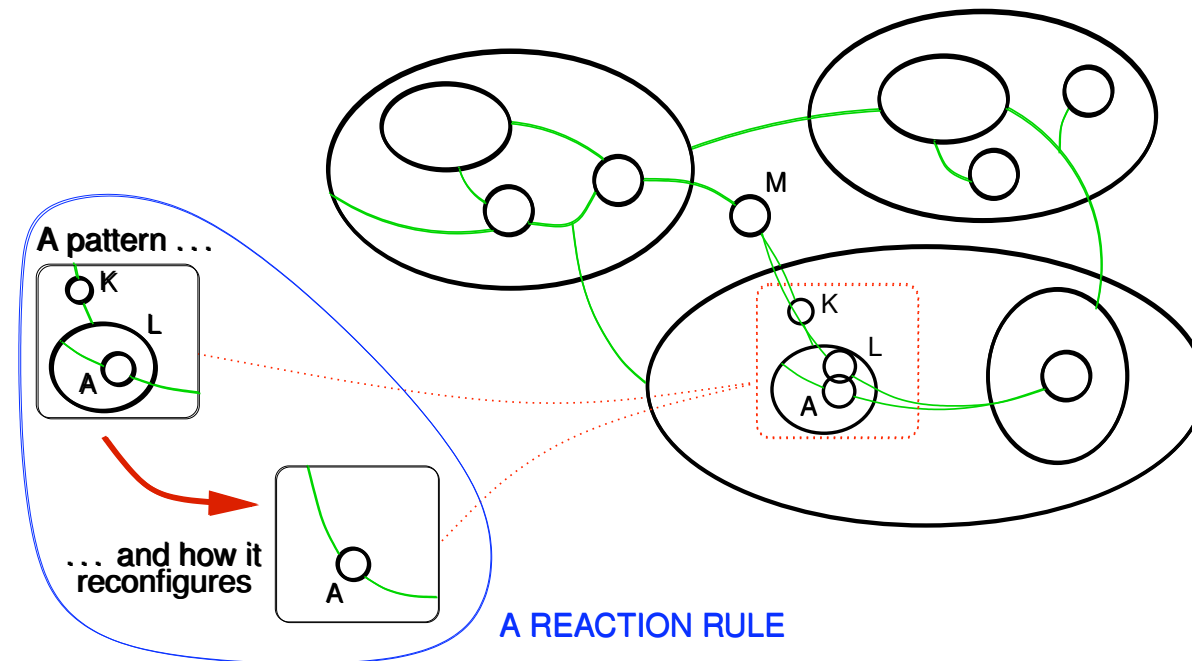


**link graph**  
 $G^L: X \rightarrow Y$



# System modification = Bigraphic rewriting

- State of the system = bigraph
- Dynamics in bigraphs = *graph rewriting rules*
- A rule can replace/move nodes, change connections, etc...





## Multi-agent Systems Design and Prototyping with Bigraphical Reactive Systems\*

Alessio Mansutti, Marino Miculan, and Marco Peressotti

## Biographical models for protein and membrane interactions

Giorgio Bacci

Davide Grohmann

Marino Miculan

## A Strategy-Based Formal Approach for Fog Systems Analysis

Souad Marir <sup>1,2,\*</sup> , Faiza Belala <sup>1</sup>  and Nabil Hameurlain <sup>2</sup> 

## Modeling Self-Adaptive Fog Systems Using Bigraphs

Hamza Sahli<sup>1</sup>, Thomas Ledoux<sup>2</sup>, and Éric Rutten<sup>3</sup>



## Modeling and Verification of Evolving Cyber-Physical Spaces

Christos Tsigkanos, Timo Kehrer, and Carlo Ghezzi  
Dipartimento di Elettronica, Informazione e Bioingegneria, Politecnico di Milano, Italy

## Bigraph Theory for Distributed and Autonomous Cyber-Physical System Design

Vincenzo Di Lecce, Alberto Amato, Alessandro Quarto *Member IAENG*, Marco Minoia




## UAV Swarms Behavior Modeling Using Tracking Bigraphical Reactive Systems

Piotr Cybulski <sup>\*</sup>  and Zbigniew Zieliński 

## Controlling resource access in Directed Bigraphs

Davide Grohmann<sup>1</sup>, Marino Miculan<sup>2</sup>

## BigraphTalk: Verified Design of IoT Applications

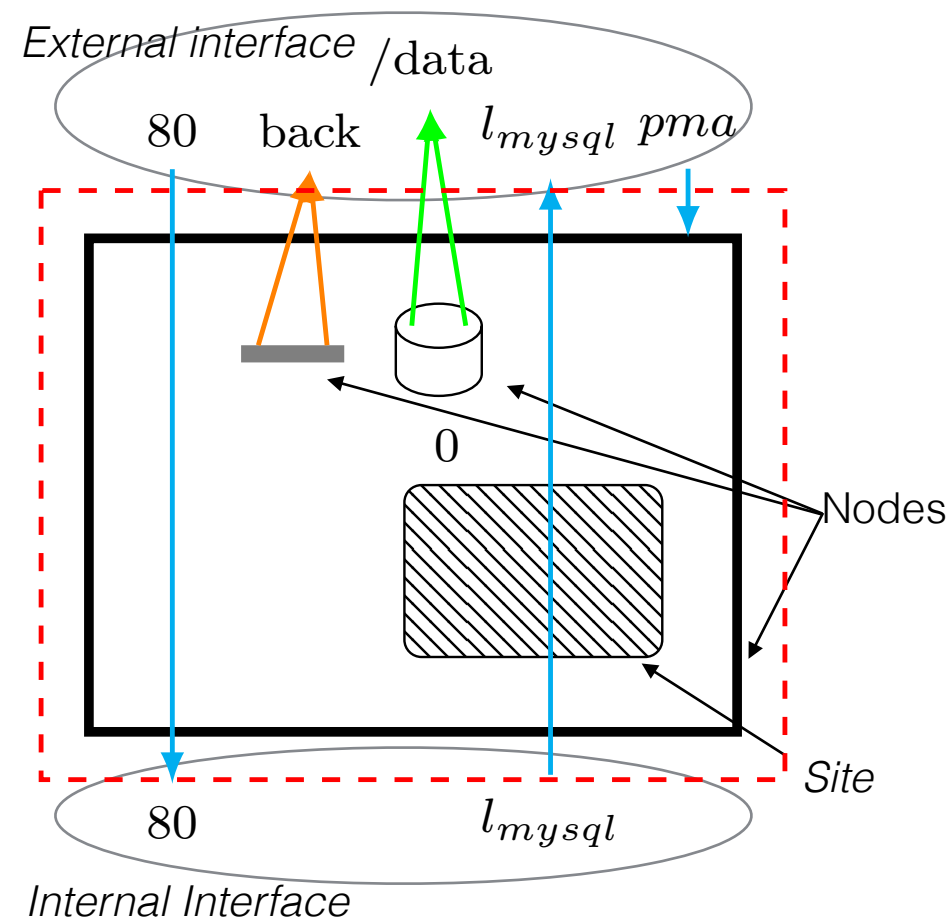
Blair Archibald , Min-Zheng Shieh , Yu-Hsuan Hu, Michele Sevegnani , and Yi-Bing Lin, *Fellow, IEEE*

## Security, cryptography and directed bigraphs

Davide Grohmann

## Local direct bigraphs [Burco, Peressotti, M., 2020]

- For containers, we have introduced **local directed bigraphs**, where
  - Nodes have assigned a type, specifying arity and polarity (represented by different shapes) and can be nested
  - *Sites* represent “holes” which can be filled with other bigraphs
  - Arcs can connect nodes to nodes (respecting polarities) or to names in *internal* and *external interfaces* (with locality)



## Local directed bigraphs – more formally

- A (*polarized*) *interface (with localities)* is a list of pairs of finite sets of names

Global names

Local names (a pair for each locality)

$$X : \langle (X_0^+, X_0^-), (X_1^+, X_1^-), \dots, (X_n^+, X_n^-) \rangle$$

$$X^+ \triangleq \biguplus_{i=1}^n X_i^+$$

$$X^- \triangleq \biguplus_{i=1}^n X_i^-$$

$$\text{width}(X) \triangleq n$$

Ascending names

Descending names

- Interfaces can be juxtaposed:

$$X \otimes Y \triangleq \langle (X_0^+ \uplus Y_0^+, X_0^- \uplus Y_0^-), (X_1^+, X_1^-), \dots, (X_n^+, X_n^-), (Y_1^+, Y_1^-), \dots, (Y_m^+, Y_m^-) \rangle$$

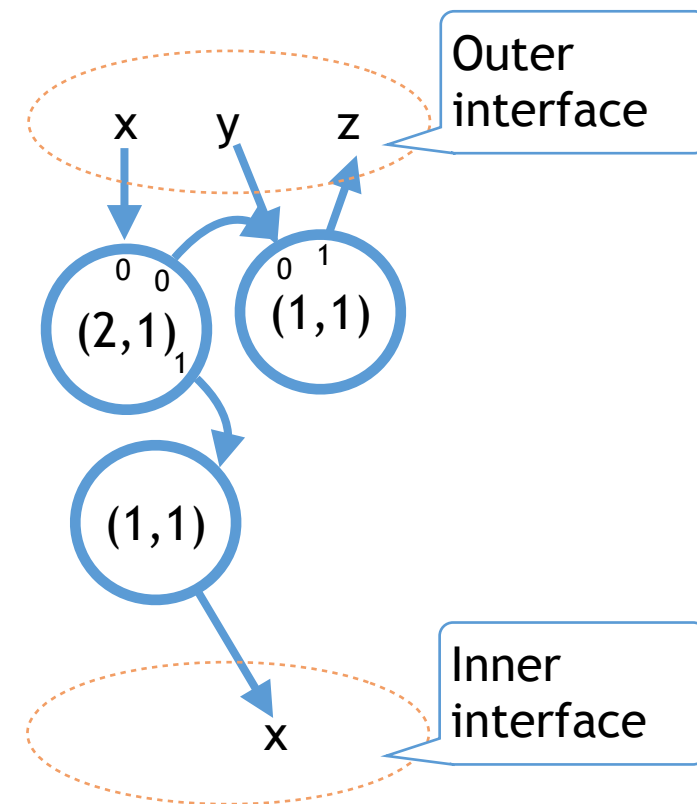
## Local interfaces are everywhere

- This system has an interface (on this side) of width=24
- Each locality (i.e. each socket) has many wires, that is, *names*
  - Ascending names = wires accessing resources outside the PC
  - Descending names = wires giving access to resources inside the PC
- Each locality is for accessing external resources (e.g. energy, mike, network, keyboard, mouse...), or to provide access to internal resources (e.g. PCIe), or both



## Local directed bigraphs – more formally

- A **signature**  $K = \{c_1, c_2, \dots\}$  is a set of controls, i.e. pairs  $c_i = (n_i^+, n_i^-)$
- Each *control* is the type of basic components, specifying inputs (positive part) and outputs (negative part)
- **Beware:** direction of arrows represents “access” or “usage” not “information flow” (somehow dual to string diagrams)
- E.g., a graph representing a system that accesses to something internal over  $x$ , something external over  $z$ , and provides services over  $x, y$





## Local directed bigraphs – more formally

- A **signature**  $K = \{c_1, c_2, \dots\}$  is a set of controls, i.e. pairs  $c_i = (n_i^+, n_i^-)$
- Given two interfaces  $I, O$ , a local directed bigraph  $B : I \rightarrow O$  is a tuple

$$B = (V, E, ctrl, prnt, link)$$

where

- $V$  = finite set of *nodes*
- $E$  = finite set of *edges*
- $ctrl : V \rightarrow K$  = *control map*: assigns each node a type, that is a number of *inward* and *outward ports*
- $prnt$ : tree-like structure between nodes
- $link$ : directed graph connecting nodes' ports and names in interfaces (respecting polarity)

## Local directed bigraphs – more formally

- Let  $K$  be a fixed signature, and  $X, Y, Z$  three interfaces.
- Given two bigraphs  $B_1 : X \rightarrow Y, B_2 : Y \rightarrow Z$  their composition is

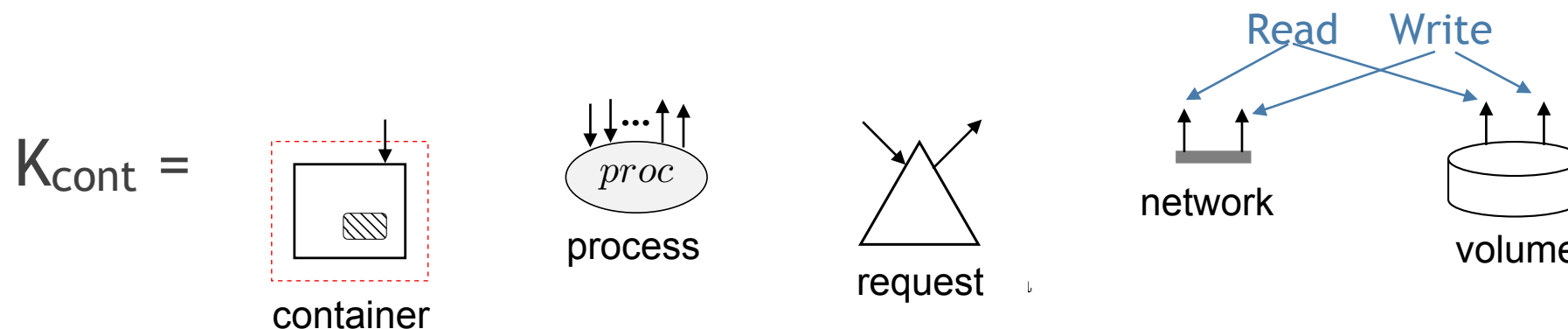
$$B_2 \circ B_1 = (V, E, ctrl, prnt, link) : X \rightarrow Z$$

defined “connecting wires” as expected

- **Monoidal category**  $(\text{Ldb}(K), \otimes, 0)$ 
  - Objects: local directed interfaces
  - Arrows: local directed bigraphs
  - Tensor: juxtaposition
- Enjoys nice properties of bigraphs (RPOs, IPOs, etc.)

## A LDB signature for containers

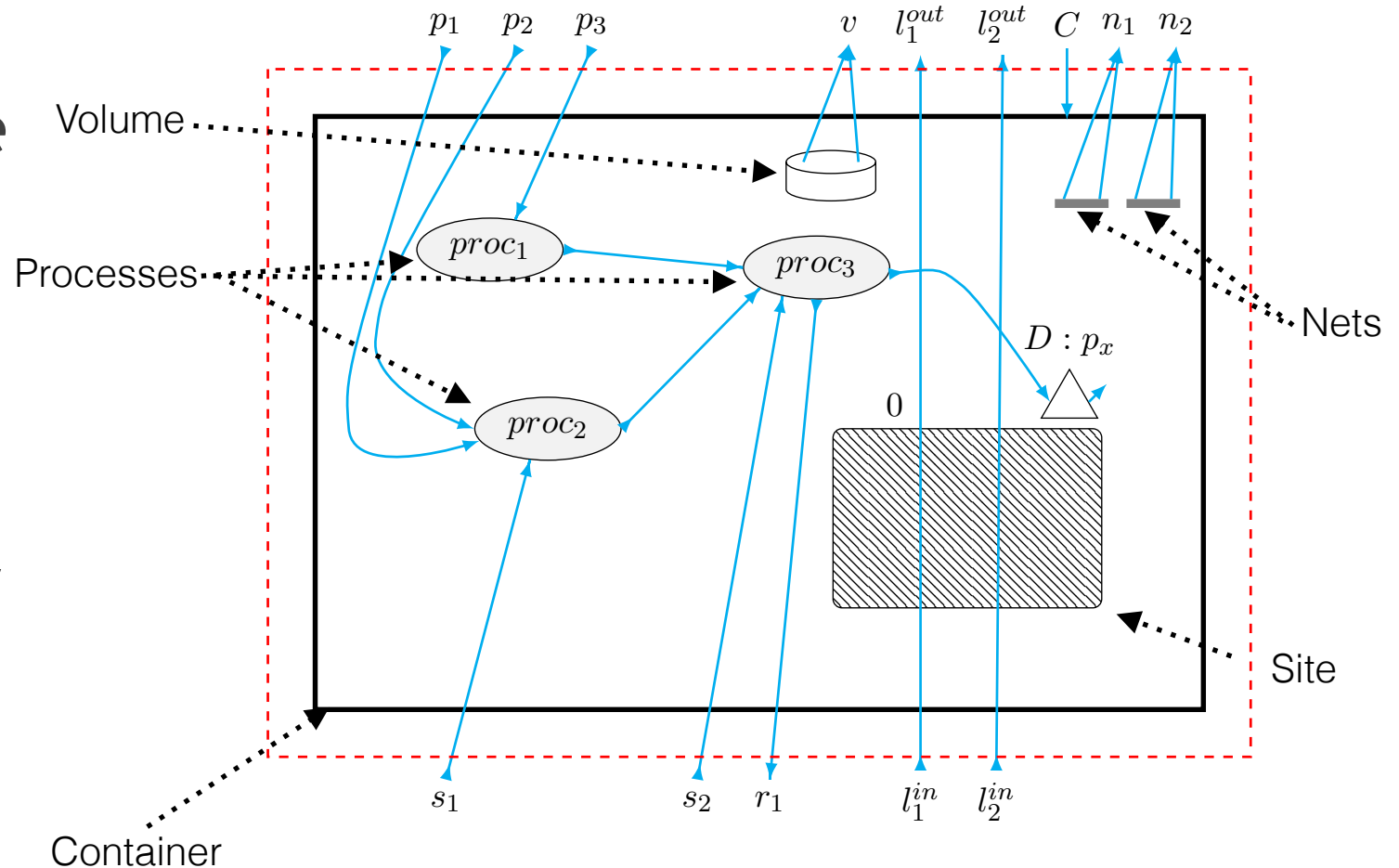
- Controls to represent main elements of a container



- shapes are only for graphical rendering
- (nodes are subject to some sorting conditions)
- Can be extended with other controls as needed (achieving *flexibility* and *openness*)
  - Changing signature = change of base in fibred category

# Containers are local directed bigraphs!

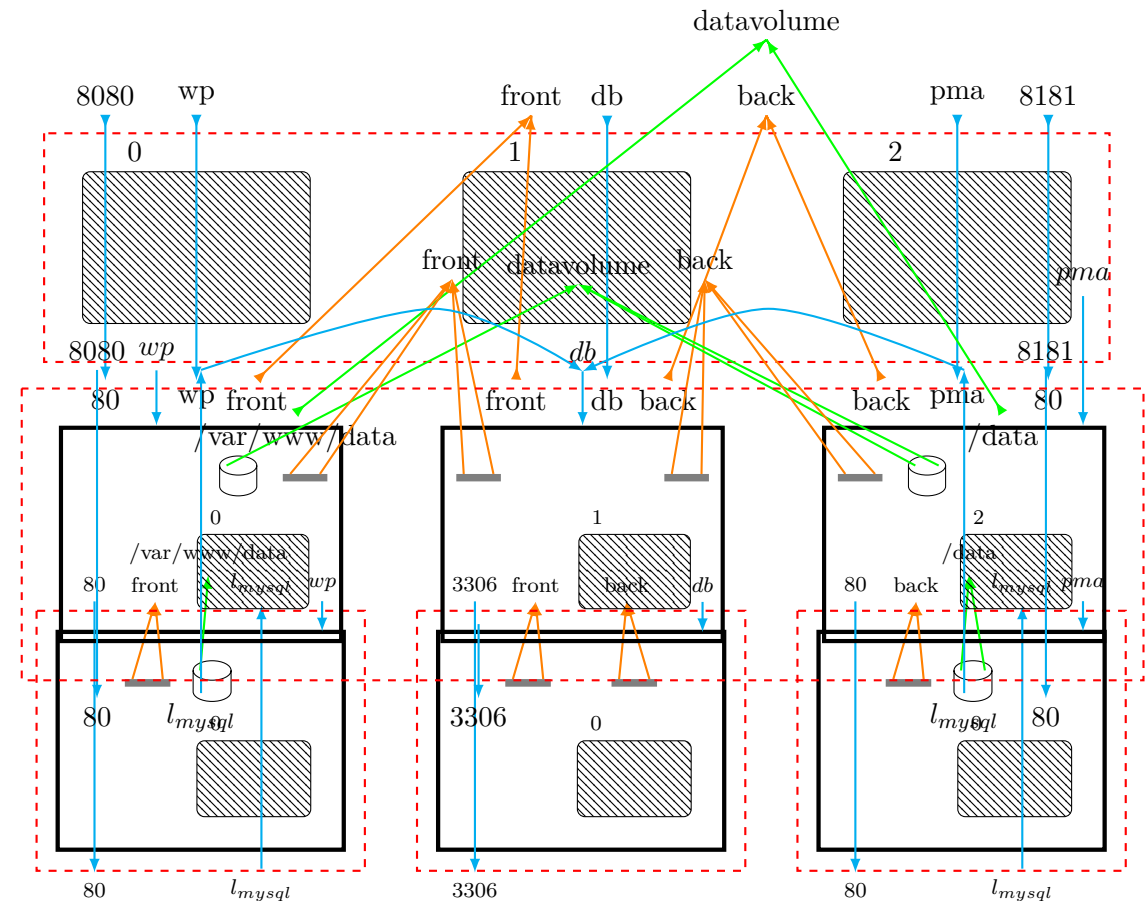
- Container = ldb whose interfaces contain the name of the container, the exposed ports, required volumes and networks, etc.
- This is not only a picture, but the graphical representation of an arrow in the category  $Ldb(K_{cont})$



$$B : \langle (\{\}, \{\}), (\{s_1, s_2, l_1^{in}, l_2^{in}\}, \{r_1\}) \rangle \rightarrow \langle (\{\}, \{\}, (\{n_1, n_2, v, l_1^{out}, l_2^{out}\}, \{p_1, p_2, p_3, C\})) \rangle$$

# And composition is another bigraph itself!

- Composition of containers as done by `docker-compose` = composition of corresponding bigraphs inside a *deployment bigraph* specifying volumes, networks, name and port remapping, etc.
  - Encoding is “functorial”
- The deployment bigraph is obtained automatically from the YAML configuration file

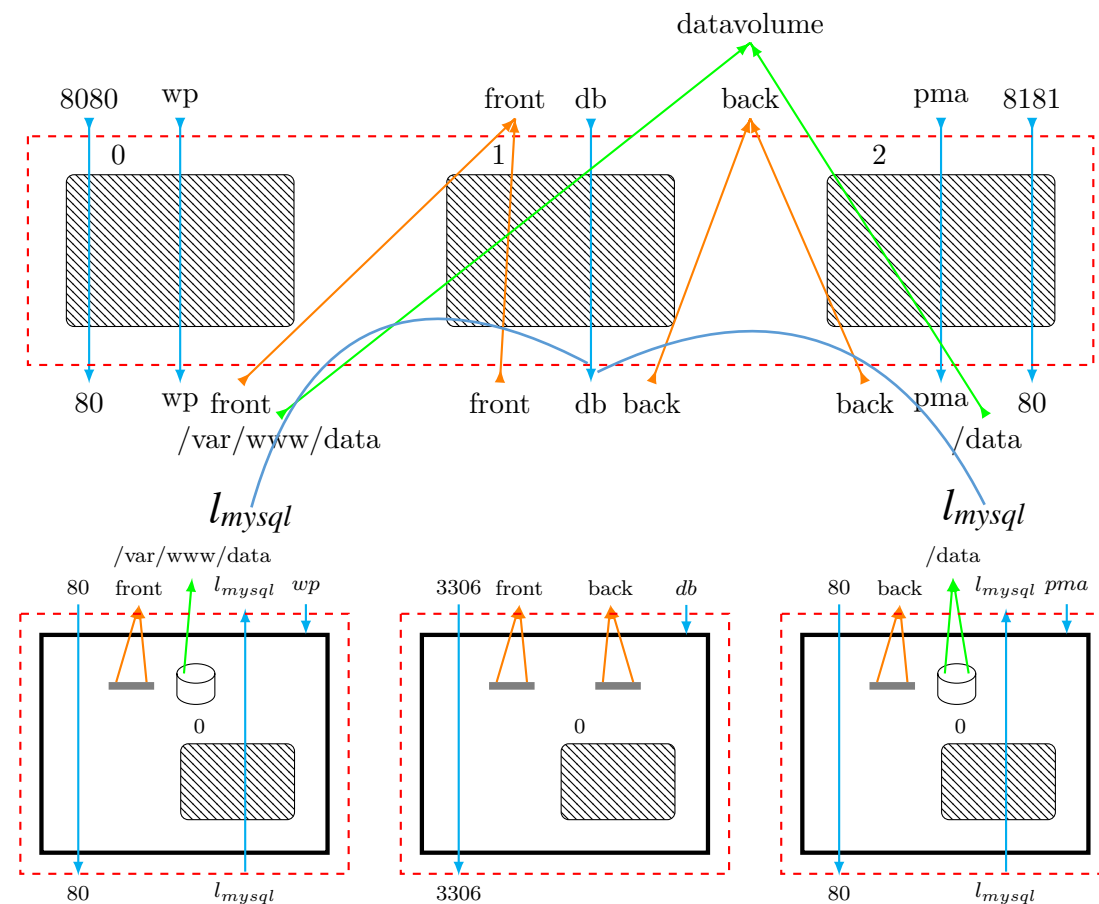


# Application: safety checks on the configuration

When represented as bigraphs, systems can be analysed using tools and techniques from graph theory

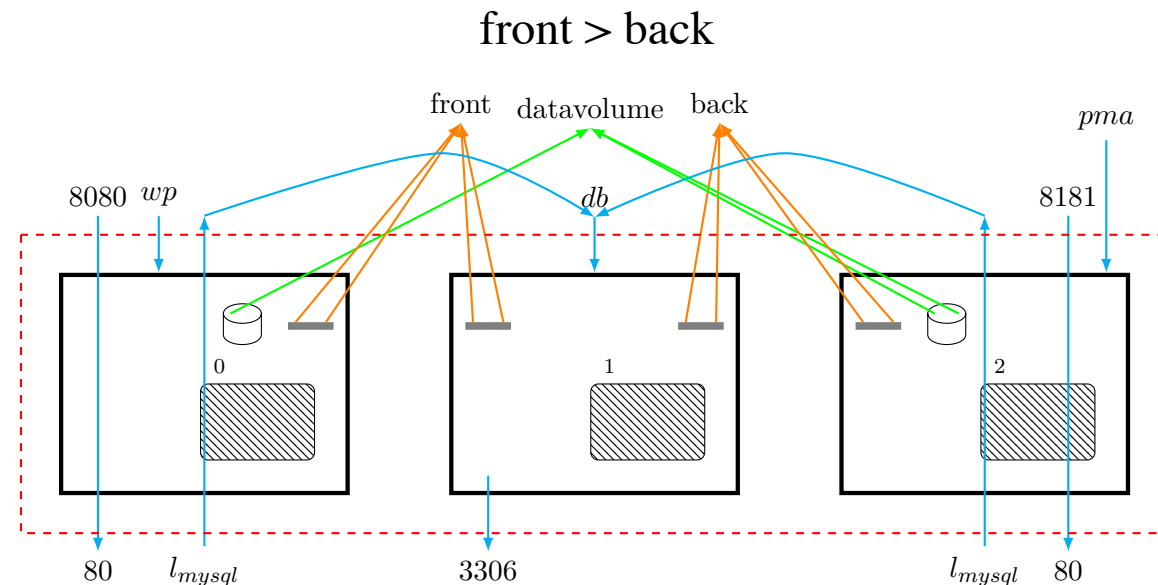
Simple example:

- **Valid links:** “if a container has a link to another one, then the two containers must be connected by at least one network”
  - Corresponds to a simple constraint on the deployment bigraph



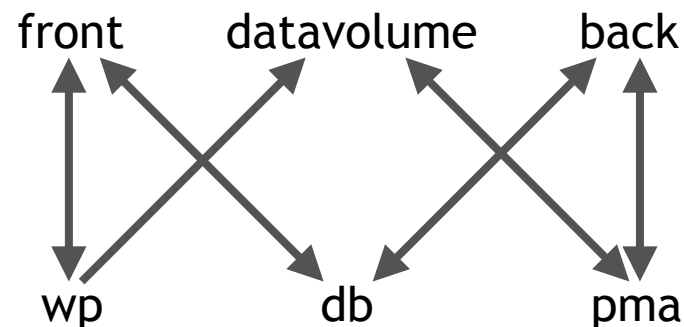
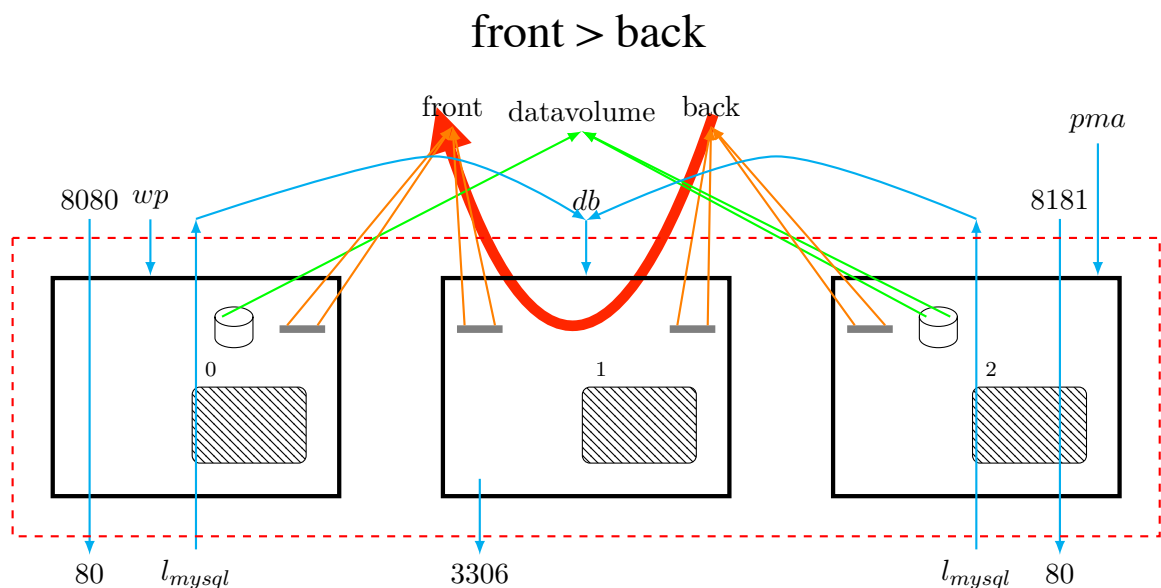
# Application: Network separation (no information leakage)

- assume that networks (or volumes) have assigned different security levels (e.g “public < guests < admin”, “back < front”).
- Security policy we aim to guarantee:
  - “Information from a higher security network cannot leak into a lower security network, even going through different containers”



# Application: Safe network separation

- Can be reduced to a *reachability problem* on an auxiliary graph representing *read-write accessibility* of containers to resources
  - The r/w accessibility graph is easily derived from the bigraph of the system
- Security policy is reduced to the property: “For each pair of resources  $m, n$  such that  $n < m$ , there is no directed path from  $n$  to  $m$ ” (i.e.,  $n$  cannot access  $m$ )
  - If this is the case, the configuration respects the security policy. Otherwise, an information leakage is possible





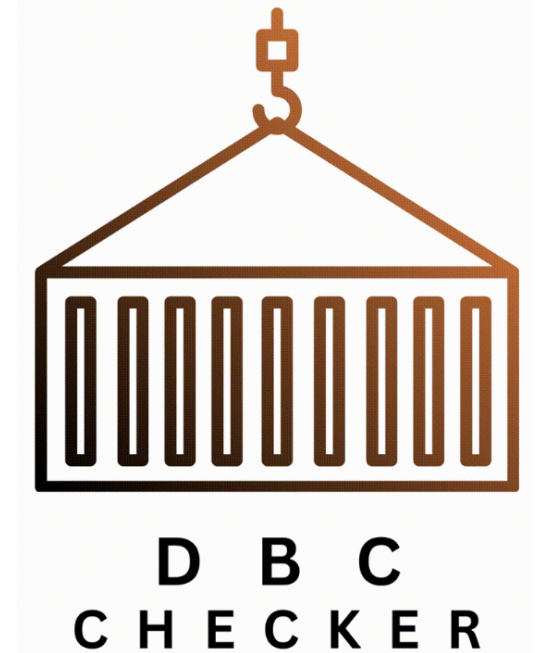
## Prototype tool: `docker2ldb`

- `docker2ldb` is a CLI tool (written in Java using the *jLibBig* library) which
  - reads a docker-compose configuration file
  - builds the corresponding deployment bigraph object
  - checks for valid connections and network separation

```
01+.back <- {0+@N_55:network, 1+@N_55:network, 0+@N_5A:network, 1+@N_5A:network}
0-@N_52:container <- {pma:i}
0-@N_53:container <- {db:i, l_db_wp:i, l_mysql_pma:i}
0-@N_54:container <- {wp:i}
0 <- {N_52:container, N_53:container, N_54:container}
N_52:container <- {N_55:network, N_57:volume, 0}
N_53:container <- {N_58:network, N_5A:network, 1}
N_54:container <- {N_5D:network, N_5B:volume, 2}
N_55:network <- {}
N_57:volume <- {}
N_58:network <- {}
N_5A:network <- {}
N_5D:network <- {}
N_5B:volume <- {}
[WARNING] Network "back" can read network "front"!
```

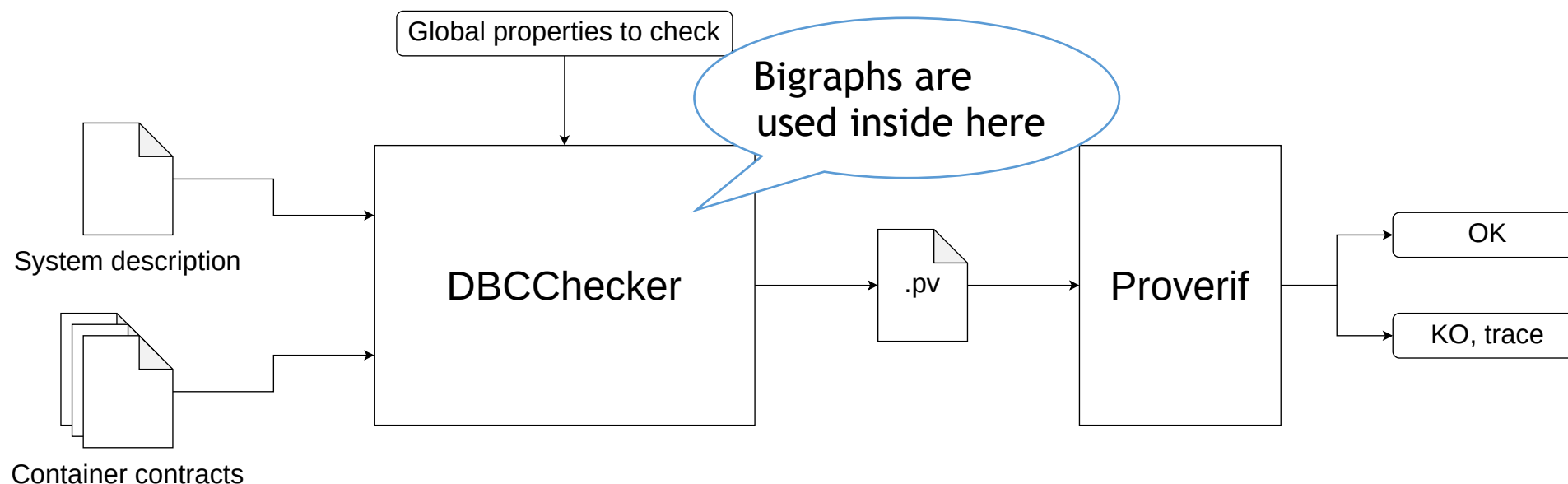
## DBCChecker [Altarui, M., Paier, 2023]

A tool that aims to verify security properties of systems obtained by composition of containers



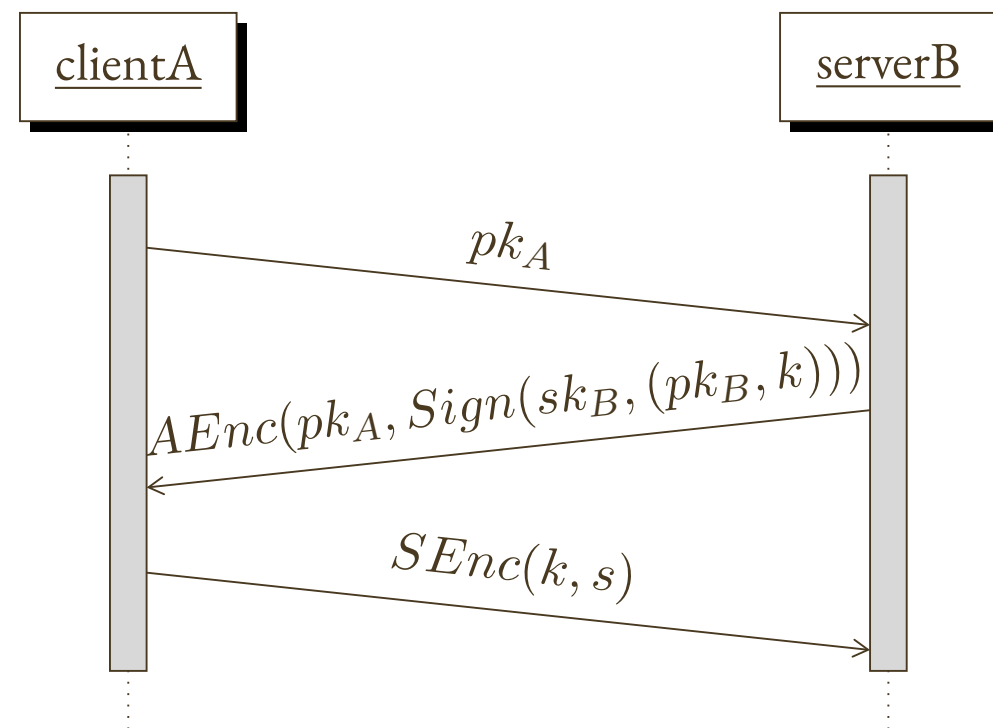
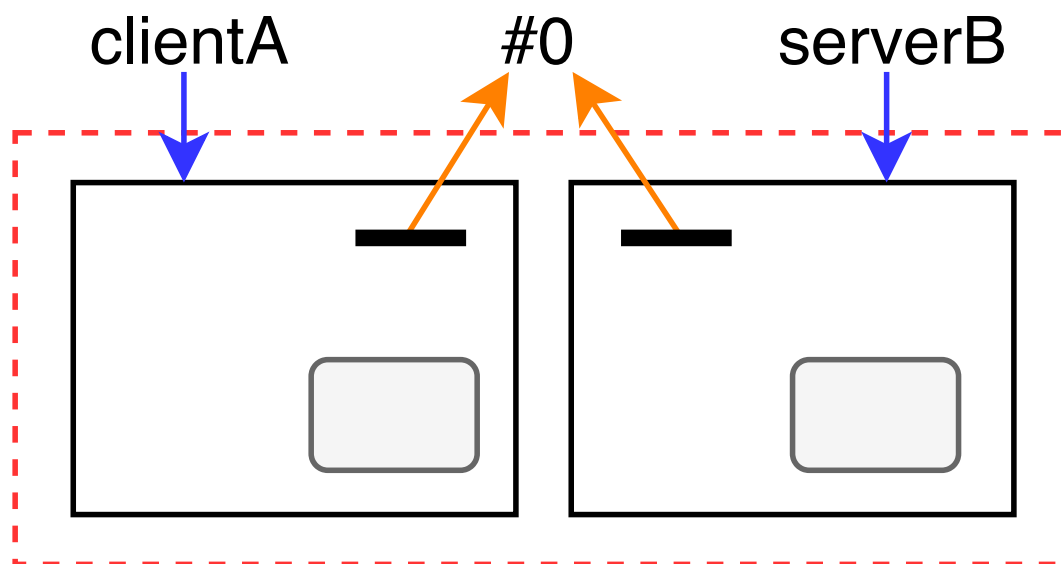
# DBCChecker

- Input:
  - a configuration of a container-based system
  - for each container, an abstract description of the interaction on its interface (“contract”)
  - Global properties to be checked
- Output: a model for the global system, verifiable in some backend

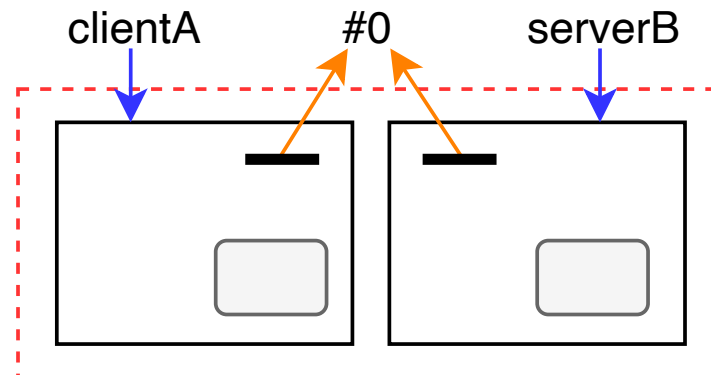


## A basic example: secure handshake

- Two containers, “client” and “server”
- Global property to check: confidentiality of message  $s$



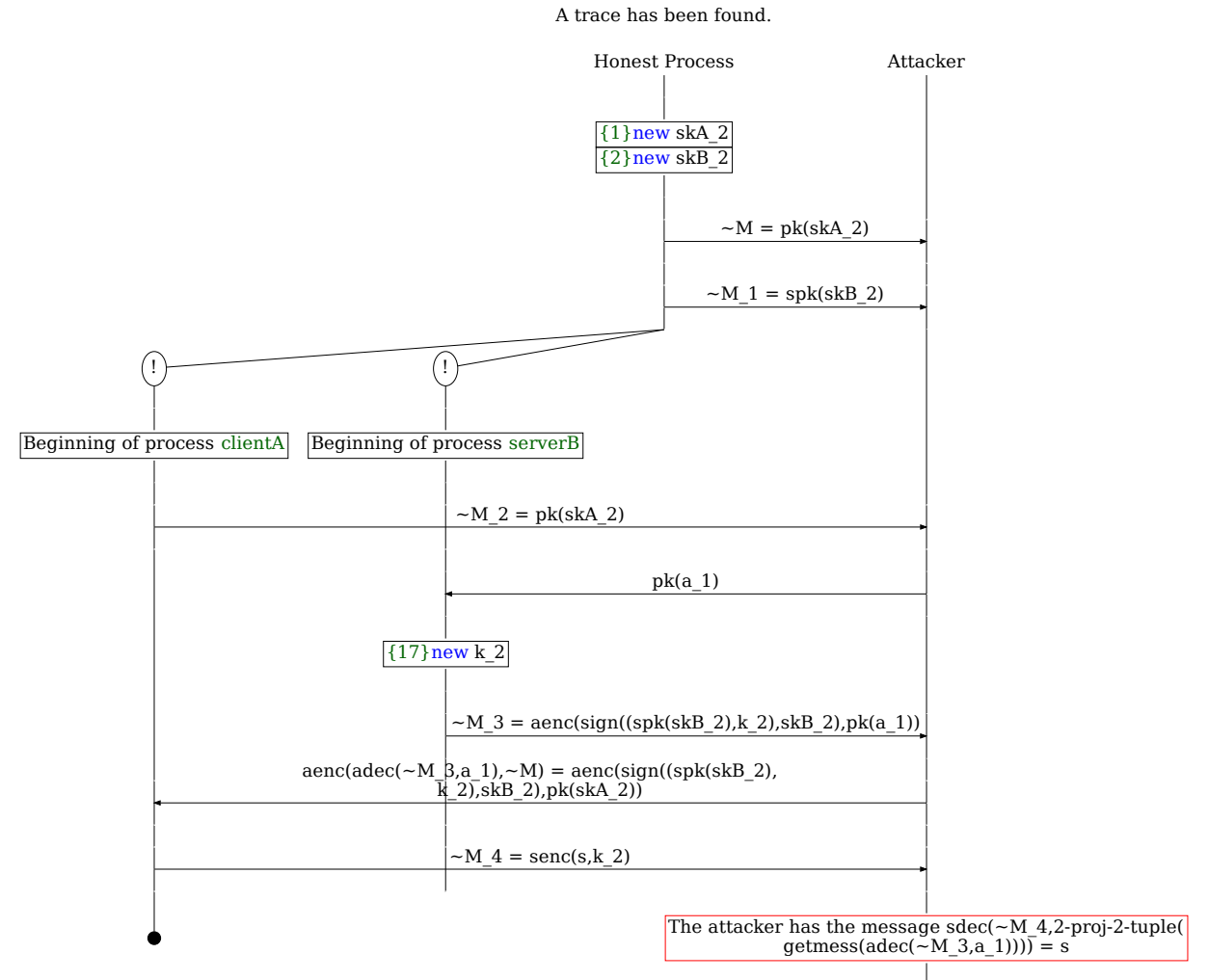
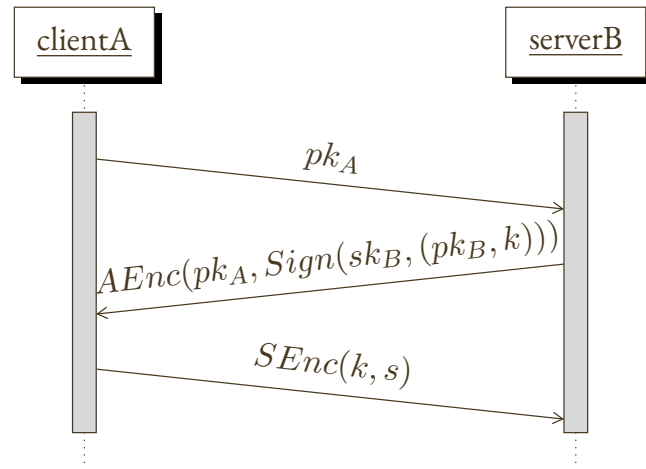
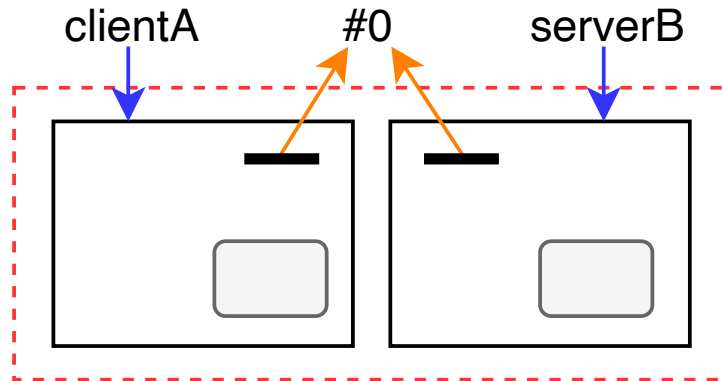
# A basic example: secure handshake: contracts



```
1  "clientA": {
2    "metadata": {
3      "type": "node",
4      "control": "1on0",
5      "params": ["pkA:pkey", "skA:skey",
6                "pkB:spkey"],
7      "behaviour": "!(out (#0+, pkA);
8                    in (#0+, x : bitstring);
9                    let y = adec(x, skA) in
10                   let (=pkB, k : key) = checksign(y,
11                                     pkB) in
12                   out (#0+, senc(s, k))).",
13      "attribute": ""
14    },
15    "label": "clientA"
16  }
```

```
1  "serverB": {
2    "metadata": {
3      "type": "node",
4      "control": "1on0",
5      "params": ["pkB:spkey", "skB:sskey"],
6      "behaviour": "!(in(#0+, pkX : pkey);
7                    new k : key;
8                    out(#0+, aenc(sign((pkB, k), skB),
9                                     pkX));
10                   in(#0+, x : bitstring);
11                   let z = sdec(x, k) in 0 ).",
12      "attribute": ""
13    },
14    "label": "serverB"
15  }
```

# A basic example: secure handshake: result



## Conclusions: some future work

- Formalisation of other static properties (Spatial logics?)
- Finer analysis of containers - i.e., identify connections between processes and resources, by code analysis
- Consider dynamics and temporal properties - in particular, *system reconfiguration*
- Integrate with runtime monitoring
  - If we observe something, which is the new configuration?
- Improve tools, UI/UX
- Quantitative aspects (e.g. fault probability estimation)
- Configuration synthesis
- The sky's is the limit!

# Epilogue

- Bigraphs are a well-suited formal metamodel for container-based systems
  - Capture logical connections of components and processes, nesting of components, composition of containers
  - Strong basis for tools and for theoretical results
  - Simple graphical language (amenable also for non experts)
  - Huge possibilities of research projects (e.g. PNRR) and industrial applications



# Thanks for your attention! Questions?



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